Dynamic Programming

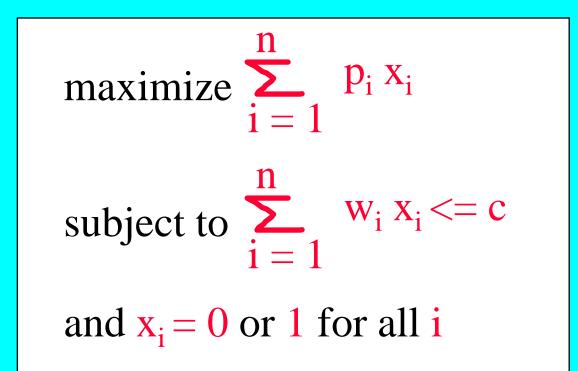
0/1 Knapsack Problem

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- Item i has a value (or profit) p_i.
- All weights and values are positive numbers.
- Hiker wants to select a subset of the **n** items such that
 - The weight of the subset should not exceed the capacity of the knapsack. (constraint)
 - Cannot select a fraction of an item. (constraint)
 - The value of the selected subset should be maximum. (optimization criterion)

0/1 Knapsack Problem

Let $x_i = 1$ when item i is selected and let $x_i = 0$ when item i is not selected.



Greedy Method 1

Be greedy on capacity utilization.

- Select items in increasing order of weight.
- n = 2, c = 7 w = [3, 6] p = [2, 10]only item 1 is selected the value of selection is 2 not best selection!

Greedy Method 2

Be greedy on the value earned.

- Select items in the decreasing order of values
- n = 3, c = 7 w = [7, 3, 2] p = [10, 8, 6]only item 1 is selected the value of selection is 10 not best selection!

Greedy Method 3

Be greedy on value density (p/w).

- Select items in decreasing order of value density.
- n = 2, c = 7 w = [1, 7] p = [10, 20]only item 1 is selected the value of selection is 10 not best selection!